

# Further study of double charmonium production in $e^+e^-$ annihilation at Belle

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We report a new analysis of double charmonium production in  $e^+e^-$  annihilation using a data sample collected by the Belle experiment. We confirm our previous observation of the processes  $e^+e^- \rightarrow J/\psi\eta_c(\chi_{c0}, \eta_c(2S))$  and perform an angular analysis for these processes. Processes of the type  $e^+e^- \rightarrow \psi(2S)(c\bar{c})_{res}$  are observed for the first time. We also observe a new charmonium state  $-X(3940)$ , produced in the process  $e^+e^- \rightarrow J/\psi X(3940)$ .

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The surprisingly large rate for processes of the type  $e^+e^- \rightarrow J/\psi\eta_c$  and  $J/\psi(c\bar{c})_{non-res}$  observed by Belle [1] remains unexplained. In the Belle analysis with a data sample of  $45\text{ fb}^{-1}$ , the presence of the process  $e^+e^- \rightarrow J/\psi\eta_c$  was inferred from the  $\eta_c$  peak in the mass spectrum of the system recoiling against the reconstructed  $J/\psi$  in inclusive  $e^+e^- \rightarrow J/\psi X$  events. Following the publication of this result, the cross-section for  $e^+e^- \rightarrow J/\psi\eta_c$  via  $e^+e^-$  annihilation into a single virtual photon was calculated to be  $\sim 2\text{ fb}$  [2], which is at least an order of magnitude smaller than the measured value. Several hypotheses have been suggested in order to resolve this discrepancy. In particular, the authors of Ref. [3] have proposed that processes proceeding via two virtual photons may be important. Other authors [4] suggest that the final states observed by Belle contain a charmonium state and a  $M \sim 3\text{ GeV}/c^2$  glueball, which are predicted by lattice QCD. Possible glueball contributions to the  $\chi_{c0}$  signal are also discussed in Ref. [5]. In this paper we report an extended analysis of the  $e^+e^- \rightarrow J/\psi(c\bar{c})_{res}$  process to check the above hypotheses and provide extra information that might be useful to resolve the puzzle. This study is performed using a data sample of  $155\text{ fb}^{-1}$  collected around the  $\Upsilon(4S)$  resonance with the Belle detector at the KEKB asymmetric energy  $e^+e^-$  storage rings.

The analysis procedure is described in detail in Refs. [1, 6]. The recoil mass  $M_{recoil}$  is defined as  $\sqrt{(E_{CM} - E_{J/\psi}^*)^2 - p_{J/\psi}^{*2}}$ , where  $E_{J/\psi}^*$  and  $p_{J/\psi}^*$  are the  $J/\psi$  center-of-mass (CM) energy and momentum, respectively. The  $M_{recoil}(J/\psi)$  spectrum for the data is presented in Fig. 1: clear peaks around the nominal  $\eta_c$  and  $\chi_{c0}$  masses are evident; another significant peak around  $\sim 3.63\text{ GeV}/c^2$  is identified as the  $\eta_c(2S)$ . The authors of Ref. [3] estimated that the two-photon-mediated process  $e^+e^- \rightarrow J/\psi J/\psi$  has a significant cross-section. To allow for a possible contribution from the exchange of two virtual photons, we fit the spectrum in Fig. 1 including all of the known narrow charmonium states below  $D\bar{D}$  threshold. The fit results are listed in Table I. The yields for  $\eta_c$ ,  $\chi_{c0}$ , and  $\eta_c(2S)$  have statistical significances

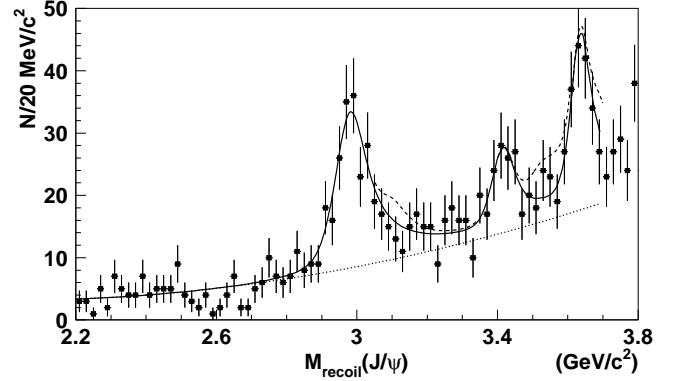


FIG. 1: The mass of the system recoiling against the reconstructed  $J/\psi$ . The curves are described in the text.

TABLE I: Summary of the signal yields ( $N$ ), charmonium masses ( $M$ ) and significances ( $\sigma$ ).

$(c\bar{c})_{res}$	$N$	$M[\text{GeV}/c^2]$	$\sigma$
$\eta_c$	$235 \pm 26$	$2.972 \pm 0.007$	10.7
$J/\psi$	$-14 \pm 20$	fixed	—
$\chi_{c0}$	$89 \pm 24$	$3.407 \pm 0.011$	3.8
$\chi_{c1} + \chi_{c2}$	$10 \pm 27$	fixed	—
$\eta_c(2S)$	$164 \pm 30$	$3.630 \pm 0.008$	6.0
$\psi(2S)$	$-26 \pm 29$	fixed	—

between 3.8 and 10.7. The fit returns negative yields for the  $J/\psi$  and  $\psi(2S)$ ; the  $\chi_{c1}$  and  $\chi_{c2}$  yields are found to be consistent with zero. A fit with all these contributions fixed at zero is shown as a solid line in Fig. 1; the dashed line in the figure corresponds to the case where the contributions of the  $J/\psi$ ,  $\chi_{c1}$ ,  $\chi_{c2}$  and  $\psi(2S)$  are set at their 90% confidence level (CL) upper limit values; the dotted line is the background function.

Given the arguments in Ref. [3], it is important to check for any momentum scale bias that may shift the recoil mass values and confuse the interpretation of peaks in the  $M_{recoil}$  spectrum. We use  $e^+e^- \rightarrow \psi(2S)\gamma$ ,

TABLE II: The  $\alpha$  parameters obtained from fits to the production and helicity angle distributions for  $e^+e^- \rightarrow J/\psi(c\bar{c})_{\text{res}}$ .

$(c\bar{c})_{\text{res}}$	Separate		Simultan.
	$\alpha_{\text{prod}}$	$\alpha_{\text{hel}}$	$\alpha_{\text{hel}} \equiv \alpha_{\text{prod}}$
$\eta_c$	$1.4^{+1.1}_{-0.8}$	$0.5^{+0.7}_{-0.5}$	$0.93^{+0.57}_{-0.47}$
$\chi_{c0}$	$-1.7^{+0.5}_{-0.5}$	$-0.7^{+0.7}_{-0.5}$	$-1.01^{+0.38}_{-0.33}$
$\eta_c(2S)$	$1.9^{+2.0}_{-1.2}$	$0.3^{+1.0}_{-0.7}$	$0.87^{+0.86}_{-0.63}$

$\psi(2S) \rightarrow J/\psi \pi^+ \pi^-$  events to calibrate and verify the recoil mass scale. From the study of the spectrum of recoil masses squared against  $\psi(2S)$  in the data, we calculate that the  $J/\psi$  recoil mass is shifted by not more than  $3 \text{ MeV}/c^2$ . As an additional cross-check we fully reconstruct double charmonium events. We find 3 pure events with  $J/\psi \eta_c$  combinations with energies consistent with total CM energy. Based on the  $\eta_c$  yield in the  $M_{\text{recoil}}(J/\psi)$  distribution, we expect  $2.6 \pm 0.8$  fully reconstructed events, consistent with the observed signal. Thus we conclude that the peak in  $M_{\text{recoil}}(J/\psi)$  is dominated by  $J/\psi \eta_c$  production. We also search for fully reconstructed events with  $J/\psi J/\psi$  combinations and find no such candidates in our data. Based on the calibration of the  $M_{\text{recoil}}(J/\psi)$  scale, the result of the fit to the  $M_{\text{recoil}}(J/\psi)$  distribution and the full reconstruction cross-check, we confirm our published observation of the process  $e^+e^- \rightarrow J/\psi \eta_c$  and rule out the suggestion of Ref. [3] that a significant fraction of the inferred  $J/\psi \eta_c$  signal might be due to  $J/\psi J/\psi$  events.

The reconstruction efficiencies for the  $J/\psi \eta_c$ ,  $J/\psi \chi_{c0}$ , and  $J/\psi \eta(2S)$  final states strongly depend on  $\theta_{\text{prod}}$ , the production angle of the  $J/\psi$  in the CM frame with respect to the beam axis, and the helicity angle  $\theta_{\text{hel}}$ . We therefore perform an angular analysis for these modes before computing cross-sections. We fit the  $M_{\text{recoil}}(J/\psi)$  distributions in bins of  $|\cos(\theta_{\text{prod}})|$  and  $|\cos(\theta_{\text{hel}})|$ , and correct the yield for the reconstruction efficiencies determined bin-by-bin from the MC. The results are plotted in Fig. 2, together with fits to functions  $A(1 + \alpha \cos^2 \theta)$  (solid lines). We also perform simultaneous fits to the production and helicity angle distributions for each of the  $(c\bar{c})_{\text{res}}$  states, assuming  $J/\psi(c\bar{c})_{\text{res}}$  production via a single virtual photon and angular momentum conservation, thus setting  $\alpha_{\text{prod}} \equiv \alpha_{\text{hel}}$ . The values of the parameter  $\alpha$  are listed in Table II. The angular distributions for the  $J/\psi \eta_c$  and  $J/\psi \eta_c(2S)$  peaks are consistent with the expectations for production of these final states via a single virtual photon,  $\alpha_{\text{prod}} = \alpha_{\text{hel}} = +1$  [2]. The prediction for a spin-0 glueball contribution ( $e^+e^- \rightarrow J/\psi \mathcal{G}_0$ ) to the  $J/\psi \eta_c$  peak,  $\alpha_{\text{prod}} = \alpha_{\text{hel}} \simeq -0.87$  [4], is disfavored. The process  $e^+e^- \rightarrow \gamma^* \rightarrow J/\psi \chi_{c0}$  can proceed via both S- and D-wave amplitudes, and predictions for the resulting angular distributions are therefore model

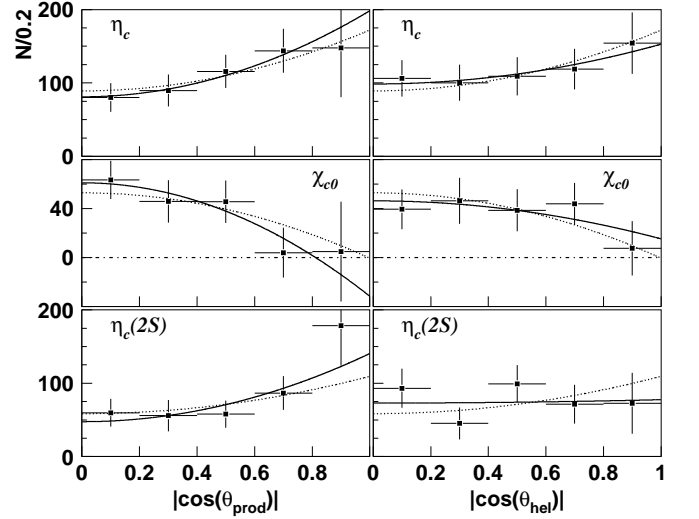


FIG. 2: Distributions of cosines of the production (left) and  $J/\psi$  helicity angles (right) for  $e^+e^- \rightarrow J/\psi \eta_c$  (top row),  $e^+e^- \rightarrow J/\psi \chi_{c0}$  (middle row),  $e^+e^- \rightarrow J/\psi \eta(2S)$  (bottom row). The solid lines are results of the individual fits; the dotted lines are the simultaneous fit results.

dependent. Our results disfavor the NRQCD expectation  $\alpha_{\text{prod}} = \alpha_{\text{hel}} \simeq 0.25$  [2, 5], and are more consistent with S-wave production, where  $\alpha_{\text{prod}} = \alpha_{\text{hel}} = -1$ .

To calculate the cross-sections we fix the production and helicity angle distributions in the MC to  $1 + \cos^2 \theta$  for  $J/\psi \eta_c(\eta_c(2S))$ , and to  $1 - \cos^2 \theta$  for  $J/\psi \chi_{c0}$ . To reduce the model dependence of our results due to the effect of initial state radiation, whose form-factor dependence on  $Q^2$  of the virtual photon is unknown, we calculate cross-sections in the Born approximation. As in Ref. [1], we present our result in terms of the product of the cross-section and the branching fraction of the recoil charmonium state into more than 2 charged tracks:  $\sigma \times \mathcal{B}_{>2}$ , where  $\mathcal{B}_{>2}((c\bar{c})_{\text{res}}) \equiv \mathcal{B}((c\bar{c})_{\text{res}} \rightarrow > 2 \text{ charged})$ . The cross-sections are given in Table IV.

We perform a similar study with reconstructed  $\psi(2S) \rightarrow J/\psi \pi^+ \pi^-$  decays to search for  $e^+e^- \rightarrow \psi(2S)(c\bar{c})_{\text{res}}$  processes. The recoil mass spectrum for the data is presented in Fig. 3: peaks corresponding to the  $\eta_c$ ,  $\chi_{c0}$ , and  $\eta_c(2S)$  can be seen. The fit to the  $M_{\text{recoil}}(\psi(2S))$  distribution is identical to the  $M_{\text{recoil}}(J/\psi)$  fit, but due to the limited sample in this case, the masses of the established charmonium states are fixed to their nominal values; the  $\eta_c(2S)$  mass is fixed to  $3.630 \text{ GeV}/c^2$  as found from the  $M_{\text{recoil}}(J/\psi)$  fit. The signal yields are listed in Table III. Significances for the individual  $\eta_c$ ,  $\chi_{c0}$ , and  $\eta_c(2S)$  peaks are in the range  $3 \sim 4\sigma$ ; the significance for  $e^+e^- \rightarrow \psi(2S)(c\bar{c})_{\text{res}}$ , where  $(c\bar{c})_{\text{res}}$  is a sum over  $\eta_c$ ,  $\chi_{c0}$ , and  $\eta_c(2S)$ , is estimated to be  $5.3\sigma$ . In Fig. 3 the result of a fit with only  $\eta_c$ ,  $\chi_{c0}$  and  $\eta_c(2S)$  contributions included is shown as a solid line; the dashed line shows the case where the  $J/\psi$ ,  $\chi_{c1}$ ,  $\chi_{c2}$ ,

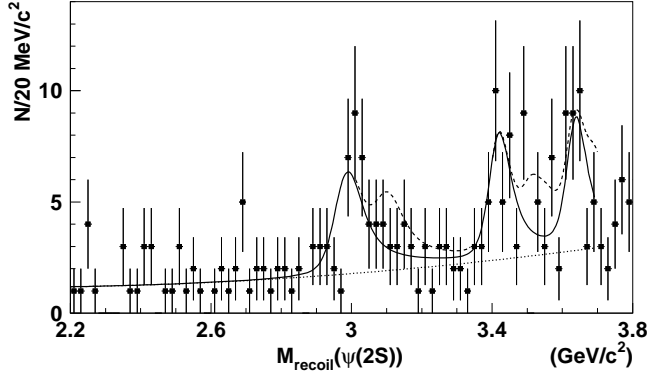


FIG. 3: The mass of the system recoiling against the reconstructed  $\psi(2S)$ . The curves are described in the text.

TABLE III: Summary of the signal yields ( $N$ ) and significances ( $\sigma$ ).

$(c\bar{c})_{\text{res}}$	$N$	$\sigma$
$\eta_c$	$36.7 \pm 10.4$	4.2
$J/\psi$	$6.9 \pm 8.9$	—
$\chi_{c0}$	$35.4 \pm 10.7$	3.5
$\chi_{c1} + \chi_{c2}$	$6.6 \pm 8.0$	—
$\eta_c(2S)$	$36.0 \pm 11.4$	3.4
$\psi(2S)$	$-8.3 \pm 8.5$	—

and  $\psi(2S)$  contributions are set at their 90% CL upper limit values; the dotted line is the background function. Finally, the calculated products of the Born cross-section and the branching fraction of the recoiling charmonium state into two or more charged tracks ( $\sigma \times \mathcal{B}_{>0}$ , where  $\mathcal{B}_{>0}((c\bar{c})_{\text{res}}) \equiv \mathcal{B}((c\bar{c})_{\text{res}} \rightarrow > 0 \text{ charged})$ ) are presented in Table IV.

Using even larger data set of  $280 \text{ fb}^{-1}$ , which became available by the summer 2004, we extend the analysis of the recoil masses against  $J/\psi$  above  $D\bar{D}$  threshold. We find another significant peak around the mass of

TABLE IV: Summary of the cross-sections for  $e^+e^- \rightarrow J/\psi (c\bar{c})_{\text{res}}$  and  $e^+e^- \rightarrow \psi(2S) (c\bar{c})_{\text{res}}$ .  $\mathcal{B}_{>2(>0)}$  denotes the branching fraction for final states containing more than 2 (at least one) charged tracks. The units are fb, and the upper limits are set at 90% CL.

$(c\bar{c})_{\text{res}}$	$\sigma_{\text{Born}} \times \mathcal{B}_{>2}$	$\sigma_{\text{Born}} \times \mathcal{B}_{>0}$
$\eta_c$	$25.6 \pm 2.8 \pm 3.4$	$16.3 \pm 4.6 \pm 3.9$
$J/\psi$	$< 9.1$	$< 16.9$
$\chi_{c0}$	$6.4 \pm 1.7 \pm 1.0$	$12.5 \pm 3.8 \pm 3.1$
$\chi_{c1} + \chi_{c2}$	$< 5.3$	$< 8.6$
$\eta_c(2S)$	$16.5 \pm 3.0 \pm 2.4$	$16.0 \pm 5.1 \pm 3.8$
$\psi(2S)$	$< 13.3$	$< 5.2$

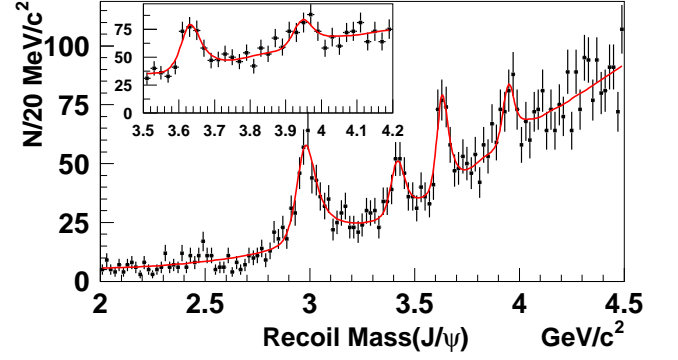


FIG. 4: The mass of the system recoiling against the reconstructed  $J/\psi$ . The curves are described in the text.

$M \sim 3.940 \text{ GeV}/c^2$  (Fig. 4). We denote this peak as  $X(3940)$ . The fit to this spectrum includes the signal function, which is a sum over four charmonium states:  $\eta_c$ ,  $\chi_{c0}$ ,  $\eta_c(2S)$ ,  $X(3940)$ , and the background function that includes also the possible contribution from  $e^+e^- \rightarrow J/\psi D\bar{D}$  events. The mass of the new charmonium state found by the fit is  $M_X = (3.940 \pm 0.012) \text{ GeV}/c^2$ ; the signal yield is  $N = 149 \pm 33$  events and the significance of the signal is  $4.5\sigma$ . The intrinsic width of the state is consistent with zero within a large error due to poor  $M_{\text{recoil}}$  resolution. We set an upper limit on  $\Gamma$  to be  $96 \text{ MeV}/c^2$  at 90% CL.

We also search for the decay of  $X(3940)$  into  $D\bar{D}^*$  and  $D\bar{D}^{*0}$  final states by reconstructing one of  $D$  mesons and requiring the second  $\bar{D}$  or  $\bar{D}^*$  in the recoil mass spectrum against reconstructed  $J/\psi D$  combinations. We find a significant signal of  $e^+e^- \rightarrow J/\psi X(3940)$  process when the event is tagged as  $X(3940) \rightarrow D\bar{D}^*$ , while no signal is found for  $X(3940) \rightarrow D\bar{D}$ . We thus conclude that the dominant  $X(3940)$  decay mode is  $D\bar{D}^*$ , and this state has a different nature from the recently found enhancement in  $J/\psi\omega$  mass distribution around the same mass [7].

In summary, using a data set of  $155 \text{ fb}^{-1}$  we confirm our published observation of  $e^+e^- \rightarrow J/\psi \eta_c$ ,  $J/\psi \chi_{c0}$  and  $J/\psi \eta_c(2S)$  and find no evidence for the process  $e^+e^- \rightarrow J/\psi J/\psi$ . We have calculated the cross-sections for  $e^+e^- \rightarrow J/\psi \eta_c$ ,  $J/\psi \chi_{c0}$ , and  $J/\psi \eta_c(2S)$  with better statistical accuracy and reduced systematic errors and set an upper limit for  $\sigma(e^+e^- \rightarrow J/\psi J/\psi) \times \mathcal{B}(J/\psi \rightarrow > 2 \text{ charged})$  of  $9.1 \text{ fb}$  at the 90% CL. Although this limit is not inconsistent with the prediction for the  $J/\psi J/\psi$  rate given in Ref. [3], the suggestion that a large fraction of the inferred  $J/\psi \eta_c$  signal consists of  $J/\psi J/\psi$  events is ruled out. We have measured the production and helicity angle distributions for  $e^+e^- \rightarrow J/\psi \eta_c$ ,  $J/\psi \chi_{c0}$ , and  $J/\psi \eta_c(2S)$ ; the distributions are consistent with expectations for these states, and disfavor a spin-0 glueball contribution to the  $\eta_c$  peak. We observe  $\psi(2S)(c\bar{c})_{\text{res}}$

production for the first time, and find that the production rates for these final states are of the same magnitude as the corresponding rates for  $J/\psi(c\bar{c})_{\text{res}}$ . Finally, using a larger data set we observe the new narrow charmonium state at the mass  $M_X = (3.940 \pm 0.012) \text{ GeV}/c^2$ .

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